Research paper

Using thermoluminescence signals from feldspars for low-temperature thermochronology

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A B S T R A C T

Natural thermoluminescence (TL) signals from feldspar crystals extracted from thermally stable drill cores (T = −4.1 to 60.2 °C) exhibit a strong dependence on geologic and laboratory thermal conditions. As burial temperature increases, the position of the TL glow curve at half-maximum intensity (i.e., the T1/2 parameter) shifts to higher measurement temperatures. This shift is also observed following isothermal treatments in the laboratory. This relationship can be explained using a kinetic model originally developed for the optical luminescence dating of feldspar grains. The thermal history of a sample is preserved in the degree of electron trap saturation as a function of thermal detrapping probability, which varies with recombination distance. A natural feldspar sample contains a range of thermal stabilities: the least stable traps will remain empty, the most stable will be full, and those traps which are partially filled, in the case of thermal equilibrium, be diagnostic of the storage temperature. The T1/2 parameter of a TL glow curve reflects which sites remain occupied. This interpretation is further borne out by additive dose measurements which illustrate that samples buried at lower temperatures are fully saturated at lower TL measurement temperatures (∼200 to 300 °C) relative to warmer samples. This signal is estimated to be useful in rapidly-cooling bedrock and should grow measurably for ∼10^2 to 10^6 years.

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1. Introduction

Luminescence signals from quartz and feldspar crystals extracted from bedrock samples have recently been shown to contain information useful for reconstructing geothermal histories (Herman et al., 2010; Li and Li, 2012; Sarkar et al., 2013; Guralnik et al., 2013, 2015a, 2015b; King et al., 2016b, c). The proposed effective closure temperatures for these signals extend below 100 °C, depending on the cooling rate and ambient temperature. Both quartz and feldspar luminescence signals face limitations, however, in their utility as thermochronometers. The fast component of optically stimulated luminescence (OSL) from bedrock quartz is characteristically dim, typically experiences dose saturation at lower doses than feldspar, and is commonly overprinted by brighter luminescence responses from inclusions, such as feldspar or zircon (Guralnik et al., 2015a). Whereas feldspar luminescence signals are brighter and saturate at higher doses than quartz, the non-first-order kinetics of detrapping (e.g., band-tail transitions, athermal fading via quantum mechanical tunneling) pose a significant challenge (Jain and Ankjaergaard, 2011; Jain et al., 2015). Luminescence signals of feldspar crystals extracted from crushed bedrock are the focus of this study.

As of yet, the only feldspar luminescence signals interrogated for thermochronometry have been the infrared stimulated luminescence (IRSL) signal from Na-feldspar, extracted from the thermally-stable KTB borehole in Germany (Guralnik et al., 2015b); the IRSL signal from surficial bedrock feldspars collected from a range of lithologies and exhumation rates (Valla et al., 2016); and IRSL signals at multiple elevated temperatures (MET) from Na- and K-rich feldspars within the rapidly-exhuming eastern Himalayan syntaxis (King et al., 2016b, c). Optically-stimulated luminescence techniques (including IRSL) offer several advantages for the luminescence dating of sediments in comparison to thermoluminescence (TL) signals: the measured signal bleaches more rapidly with sunlight exposure, and single grains can be individually stimulated with focused laser beams. However, for monitoring the dose response in a lightless but thermally-varying system, the TL signal
may provide a distinct advantage. Specifically, the stimulating energy gradually increases during the measurement procedure, which produces luminescence from a continuum of thermal stabilities in a single glow curve (Strickertson, 1985; Balescu et al., 1997). Unlike IRSL techniques, which stimulate with a constant optical power, TL is measured by gradually heating a sample from room temperature until the relevant traps are emptied (conventionally to a maximum of around 500 °C), and the luminescence emissions are monitored as a function of the temperature of the sample. Thermoluminescence emissions therefore reflect the range of occupied trap stabilities that have naturally accumulated. This study aims to characterize feldspar TL as a record of geothermal history.

Thermoluminescence has long been used to discern features about a sample’s thermal history. Most often, researchers are interested in the time since the thermal-resetting of archaeological materials. Quartz is the more common target mineral in this context. Target materials include fired ceramics (Aitken et al., 1964; Fleming et al., 1970), hearth stones (Plachy and Sutton, 1982), and burnt flint (Valladas and Valladas, 1987). A notable exception is the use of feldspar TL for the dating of burnt stones and ceramics (Mejdahl, 1983, 1985; Spencer and Sanderson, 1994, 2012). While the use of feldspar for thermoluminescence studies usually consider the decay of peaks in quartz crystals (e.g., Tang and Li, 2015), Prokein and Wagner (1994) observed the reduction of the quartz 325 °C TL peak over a wide range of steady-state temperatures (14–56 °C), and Nambo et al. (1996) made the more general observation of decreasing overall quartz TL intensity with burial temperature, an observation that was given more general observation of decreasing overall quartz TL intensity by incorporating recent advances in the understanding of feldspar luminescence kinetics (e.g., detrapping by tunneling to nearby recombination centers; Jain et al., 2015) and by considering long-term storage of feldspars at upper-crustal temperatures in terrestrial drill cores.

This study examines both the natural and laboratory-induced TL signals from feldspar crystals extracted from split drill cores originally collected from Alaska, Colorado, and Wyoming that represent steady-state heat flows of 54.4, 58.3, and 100.4 mW/m², respectively. First, the TL signals of feldspars taken from different depths were measured. The natural signals are presented along with multiple-aliquot additive-dose (MAAD) and single-aliquot regenerative (SAR) dose responses, as well as isothermal decay measurements. Next, these signals are compared with results from a kinetic model similar to that of Jain et al. (2015) which assumes that: a) distance-dependent, excited-state tunneling is the primary pathway for feldspar luminescence; and b) that sites at increasing distances from centers will exhibit greater trapping stability. We simulate laboratory and natural isothermal conditions and compare the simulated results to our measurements. Finally, we suggest future research directions.

2. Materials and methods

2.1. Geologic context and sample collection

A total of 20 samples were collected from split drill cores kept at the United States Geologic Survey Core Research Center (CRC), Lakewood, Colorado. The samples were chosen to represent a wide range of steady-state temperatures (–4.1 – 60.2 °C), within relatively uniform lithologies. The three cores sampled were from the North Slope of Alaska (CRC library code E802; n = 5; 69°50′18″N, 155°39′24″W), the Piceance Basin of northwestern Colorado (W219; n = 8; 39°53′36″N, 108°32′37″W), and the Greater Green River Basin of south-central Wyoming (R716; n = 7; 41°24′1N, 108°6′39″W) (Fig. 1(a) and (b)).

Core E802 from the Colville Basin of North Slope Alaska is comprised of the Nanushuk Group: Lower and Upper Cretaceous sandstone, shale, and minor conglomerate deltaic wedge, all shed from the Brooks Range, a series of thrust sheets stacked during the Late Jurassic to Early Cretaceous arc-continent collision (Mull et al., 1987). Core W219 is comprised of the Green River Formation: Eocene interbedded mudstone and sandstone, carbonaceous shale, lenticular sandstones and thickly-bedded evaporites that were deposited in and around lacustrine basins formed during the Laramide orogeny (Irwin, 1977; Smith et al., 2008). Core R716 contains Eocene basin-fill (Wasatch Formation): floodplain deposits of lenticular of parallel-bedded sandstones, and mudstone (Roehler, 1992). Similar to W219, the R716 core was likely derived from Laramide basement (Fan et al., 2011).

To estimate the undisturbed modern subsurface temperatures for each core, the following steps were taken. For E802, the geothermal gradients above and below the ice-bearing permafrost layer were interpolated from nearby sites within the Colville Basin which were measured for a high-resolution temperature survey of wells considered to be in thermal equilibrium (Collett et al., 1993). For W219, a similar interpolation was performed using gradient-at-depth measurements from nearby sites within the Piceance Basin (Blackwell et al., 2011). For R716, a geothermal gradient map was used (Finn, 2005). From these geothermal gradient approximations, the modern temperature of each core sample was estimated (Fig. 1(b)). Further details about these measurements can be found in the Supplementary Materials.

Whether samples are in thermal equilibrium depends on the exhumation rate at each core site. The most rapid exhumation is at site W219. Although no measurements have been made at the core site itself, fluid inclusion microthermometry (Fall et al., 2012, 2015) and vitrine reflectance data (Zhang et al., 2008) from the center of the Piceance Basin imply an exhumation rate of 0.16–0.24 km/Ma since 10 Ma, corresponding to a cooling rate of 3.8 °C/Ma within the Mesaverde Group (modern geothermal gradient of 53 °C/km), immediately below the Wasatch Formation (vitrine reflectance data suggest heat-flow values similar to modern since the Miocene). Moreover, the exhumation at the northern basin edge is expected to be slower than in the center (Zhang et al., 2008). Based on apatite fission track cooling ages, the exhumation rate for the Colville Basin (core E802) since the Paleocene has been about 0.05–0.06 km/Ma (Cole et al., 1997) and vitrine reflectance data suggest an exhumation rate of 0.01–0.02 km/Ma since the Eocene for the Green River Basin (core R716) (Jagniecki et al., 2013), both of which are effectively static for the TL signal considered here. The modern geothermal gradients at these sites are also much lower than at W219: 34 and 35°C/km compared with 53°C/km (see
Supplementary Materials for more detail), which would result in cooling rates of 1.9 and 0.5°C/Ma for E802 and R716, respectively. Because these cooling rates are considerably lower than the reported detectable cooling rates for other trapped-charge thermochronometric systems (e.g., >20–615°C/C14; Table 2 of King et al., 2016a), the modern undisturbed core temperature measurements are reported as ‘steady-state’ temperatures (TSS) hereafter.

2.2. Sample preparation and instrumentation

To isolate the inner portion of the split drill cores, the samples were spray-painted and then the outer surfaces were removed using a rotary tool fitted with a tile-cutting bit. The unexposed inner portions from the drill core samples were then ground with a pestle and mortar and sieved to isolate the 175–400 μm size fraction. These separates were then treated with 3% hydrochloric acid and separated by density using lithium metatungstate heavy liquid (ρ < 2.565 g/cm³; Rhodes, 2015) in order to isolate the most potassic feldspar crystals. Crystals were mounted on stainless steel discs in a small-diameter (3–5 mm) monolayer using silicon oil.

The outer portions of each sample were analyzed with inductively-coupled plasma mass spectrometry (ICP-MS) to estimate the U and Th contents, and with inductively-coupled optical emission spectrometry (ICP-OES) to measure the K content. These values were converted into a geologic dose-rate using the factors of Adamiec and Aiken (1998). We estimate an internal dose-rate assuming a feldspar potassium content of 12.5 ± 0.5 wt% (Huntley and Baril, 1997). Beta attenuation is calculated assuming a water content of 0.5 ± 0.5%. The resulting geologic dose-rate values are listed in Table 1.

Luminescence measurements were carried out at the UCLA luminescence laboratory using a TL-DA-20 Risø automated reader equipped with a 90Sr/90Y beta source. Thermoluminescence emissions were detected through a Schott BG3–BG39 filter combination (transmission window of 325–475 nm) in a nitrogen atmosphere.

3. Thermoluminescence signals from feldspars extracted from drill cores

3.1. Natural signals

Sixteen of the 20 measured samples produced natural TL signals suitable for analysis (Fig. 2). The four rejected samples were from core W219, were buried at temperatures >23°C, and yielded natural signals dominated by black-body radiation (approximated by measuring TL from the same aliquot after the natural signal has been removed). This lack of natural signal likely results from the high burial temperatures experienced by these samples. In core R716, however, samples with higher TSS values retained natural TL signals above black-body radiation levels. The natural variability in the upper limit of resolvable TSS values deserves further exploration.

Because the low-temperature TL peak in feldspar is generally asymmetric with overlapping peaks at higher temperatures, it is common practice to describe natural TL curves according to the measurement temperature at half of the maximum TL intensity (i.e., the position of the ‘leading edge’ of the main peak in a TL glow curve), or T1/2 (e.g., Spencer and Sanderson, 2012). As steady-state temperatures (TSS) increase, the natural T1/2 values shift to higher temperatures (Fig. 1c). Additionally, within a given core (each of which has a fairly uniform lithology), TL brightness tends to decrease at higher TSS values (Fig. 2).

3.2. Field saturation

A primary concern when considering the dose-response characteristics of luminescence signals is a change in sensitivity during the course of a measurement sequence (Wintle and Huntley, 1982). To avoid any such changes in the dose-response sensitivity induced
by heating, we tested the level of natural dose-saturation (i.e., ‘field saturation’; Kars et al., 2008) in samples J1012 and J1030 by using a multiple-aliquot additive-dose (MAAD) approach. Separate aliquots were given beta doses in addition to their natural doses. The subsequent TL curves (Fig. 3a - b) show which regions of the glow curve are saturated (and do not, therefore, grow with dose) and which regions are not saturated (and grow with dose).

Sample J1012 is almost fully saturated from about 270 to 370 °C, with an average ratio of 0.95 ± 0.02. Sample J1030 shows a similar degree of saturation, 0.95 ± 0.03, from 340 to 410 °C (Fig. 3c). The key observation from this experiment is that $T_{SS}$ relates to the TL measurement temperature at which traps are fully saturated (i.e., in field saturation; $T_{SS} = -4.1^\circ$ C for J1012 and 55.1°C for J1030). This indicates that burial temperature controls which regions within a TL curve are stable enough to accumulate charge over time. At higher measurement temperatures, both samples show ratios greater than one, which may reflect the effect of dose-quenching (for a detailed description of this phenomenon in quartz, see Bailey, 2001) on a high-temperature peak (e.g., 410 °C TL peak; Murray et al., 2009). Why the samples are $>1$ at different temperatures is unclear, but likely relates to the variability in the position of the high-temperature peak(s).

### 3.3. Signals following isothermal treatments

After the measurement of the natural signal, an aliquot of sample J1012 (core E802) was given a beta dose of 24 Gy and then subjected to a series of isothermal treatments: 50, 100, 150, and 200 °C for 10, 30, 100, 300, and 1000 s. Following these treatments, the TL signals were measured (Fig. 4). A shift to higher temperatures for the $T_{1/2}$ value and a reduction in TL intensity result from longer heat treatments and greater hold temperatures, an observation made previously (e.g., Spencer and Sanderson, 1994). This resembles the effect of burial at higher natural $T_{SS}$ values (Fig. 2).

Both of these effects are simulated later in this work in sections 4.3 and 4.4.

A higher temperature peak is evident, centered around 390 °C. High-temperature peaks (centered between ~ 310–410°C) are well-documented for feldspar TL studies and exhibit different luminescence properties than the lower-temperature peak and probably therefore involve a different combination of traps and/or

### Table 1

Sample depths, steady-state temperatures, and dose-rate information.

<table>
<thead>
<tr>
<th>Field code</th>
<th>Lab code</th>
<th>Depth (m)</th>
<th>$T_{SS}$ (°C)</th>
<th>K (%)</th>
<th>Th (ppm)</th>
<th>U (ppm)</th>
<th>Total dose-rate (Gy/ka)</th>
</tr>
</thead>
<tbody>
<tr>
<td>E802-1</td>
<td>J1012</td>
<td>159</td>
<td>-4.1</td>
<td>1.1</td>
<td>5.2</td>
<td>2.04</td>
<td>2.85 ± 0.11</td>
</tr>
<tr>
<td>E802-2</td>
<td>J1013</td>
<td>303</td>
<td>0.8</td>
<td>0.9</td>
<td>3.5</td>
<td>1.39</td>
<td>2.39 ± 0.10</td>
</tr>
<tr>
<td>E802-3</td>
<td>J1014</td>
<td>367</td>
<td>3.0</td>
<td>1.1</td>
<td>4.9</td>
<td>1.77</td>
<td>2.76 ± 0.11</td>
</tr>
<tr>
<td>E802-4</td>
<td>J1015</td>
<td>456</td>
<td>7.4</td>
<td>1.3</td>
<td>5.5</td>
<td>1.96</td>
<td>3.04 ± 0.12</td>
</tr>
<tr>
<td>E802-5</td>
<td>J1016</td>
<td>656</td>
<td>12.8</td>
<td>0.9</td>
<td>6.1</td>
<td>2.09</td>
<td>2.73 ± 0.10</td>
</tr>
<tr>
<td>W219-1</td>
<td>J1017</td>
<td>7</td>
<td>6.4</td>
<td>3.6</td>
<td>9.7</td>
<td>2.39</td>
<td>5.72 ± 0.27</td>
</tr>
<tr>
<td>W219-2</td>
<td>J1018</td>
<td>72</td>
<td>9.8</td>
<td>2.4</td>
<td>10.0</td>
<td>1.87</td>
<td>4.36 ± 0.19</td>
</tr>
<tr>
<td>W219-3</td>
<td>J1019</td>
<td>150</td>
<td>14.0</td>
<td>6.1</td>
<td>7.2</td>
<td>2.13</td>
<td>7.71 ± 0.43</td>
</tr>
<tr>
<td>W219-4</td>
<td>J1020</td>
<td>240</td>
<td>18.7</td>
<td>1.3</td>
<td>4.6</td>
<td>4.21</td>
<td>3.49 ± 0.13</td>
</tr>
<tr>
<td>W219-5</td>
<td>J1021</td>
<td>321</td>
<td>23.0</td>
<td>1.6</td>
<td>3.5</td>
<td>2.34</td>
<td>3.27 ± 0.14</td>
</tr>
<tr>
<td>W219-6</td>
<td>J1022</td>
<td>418</td>
<td>28.2</td>
<td>1.3</td>
<td>4.8</td>
<td>2.47</td>
<td>3.11 ± 0.12</td>
</tr>
<tr>
<td>W219-7</td>
<td>J1023</td>
<td>509</td>
<td>33.0</td>
<td>2.2</td>
<td>12.1</td>
<td>3.55</td>
<td>4.70 ± 0.18</td>
</tr>
<tr>
<td>W219-8</td>
<td>J1024</td>
<td>575</td>
<td>36.5</td>
<td>0.4</td>
<td>1.9</td>
<td>0.98</td>
<td>1.72 ± 0.08</td>
</tr>
</tbody>
</table>

*The natural signals from these samples were conflated with black-body radiation emissions during measurement and are disregarded from further analysis.*
The ratios of the natural response to the added-dose response are plotted as a function of measurement temperature for both samples. A ratio of 1 (dashed line) indicates that the sample is in complete field saturation. Notice how the colder sample is nearly saturated (ratio ~ 0.95) at lower measurement temperatures and saturation occurs at higher measurement temperatures for the sample with a higher burial temperature. Above about 375 °C, we see a slight rise in the ratio, which may be attributed to the behavior of a separate, high-temperature peak (Duller, 1997; Murray et al., 2009). (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

4. A kinematic model of feldspar TL

4.1. Model description

In this study, we estimate the net change in the concentration of trapped electrons with the following expression

$$\frac{dn(r')}{dt} = \frac{D}{D_0} (N(r') - n(r')) - n(r') \exp(-\Delta E/k_B T) \frac{P(r')s}{P(r') + s}$$  \hspace{1cm} (1)

The accumulation term for every dimensionless recombination distance $r'$ depends on the concentration of unoccupied traps $(N(r') - n(r'))$, which will fill at a rate proportional to the dose-rate $D$ (Gy/s), normalized by $D_0$, the dose (Gy) at which $(1 - e^{-1})$ of the total traps are filled (i.e., the characteristic dose) (Christodoulides et al., 1971). The total concentration of traps separated from a recombination center by some distance between $r'$ and $r' + dr'$ is given by Huntley (2006) as

$$N(r')dr' = N \cdot 3 \cdot (r')^2 \exp\left(-r'^3\right) dr'$$  \hspace{1cm} (2)

The loss term multiplies the concentration of trapped electrons at some distance $n(r')$ by their recombination probability. Following recent work (Jain et al., 2015; Pagonis et al., 2016), we approximate the detrapping probability in feldspar as localized transitions to randomly-distributed luminescence centers. This probability is governed by the activation energy from the ground-to the excited-state, $\Delta E$ (eV), the temperature of the lattice, $T$ (K), the attempt-to-escape frequency factor, $s$ (s$^{-1}$), and the excited-state tunneling probability, $P(r')$ (s$^{-1}$). The tunneling probability decreases with $r'$ according to the relationship

$$P(r') = P_0 \exp(-\rho' r'^{-1/3})$$  \hspace{1cm} (3)

where $P_0$ (s$^{-1}$) is the attempt-to-tunnel probability and $\rho'$ the dimensionless concentration of recombination centers in the lattice (Huntley, 2006). A more complete model description is found in the Supplementary Materials.

By numerically solving Equation (1) for geothermal or laboratory conditions, we can evaluate how the trapped electron population, $n(r')$, evolves through time (all simulations presented in this work were evaluated with the ode23tb solver within MATLAB). The resulting $n(r')$ array can then be taken as the input for a simulated TL measurement. The expression for TL intensity as a function of measurement time is given as

$$I_{TL}(t) = \int_{t_0}^{\infty} \int_{r'=0}^{\infty} n(r')dr'dt$$  \hspace{1cm} (4)

Recombination centers (Balescu et al., 1991; Duller, 1994, 1997; Murray et al., 2009). For that reason, our analysis is restricted to those regions unaffected by this higher-temperature peak.

Fig. 4. (a) Measured TL curves are shown for sample J1012 (core E802), following isothermal treatments of durations 10, 30, 100, 300, and 1000 s at holding temperatures of 50 (purple curves), 100 (blue), 150 (green), and 200 °C (orange). (b) The TL $T_{1/2}$ values of these measurements are plotted as a function of hold time and colored according to hold temperature. Notice the shift towards higher $T_{1/2}$ values with longer hold times and higher temperatures. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)
when a sample is heated from \( T = 0 \) to \( T_F \) at \( \frac{dT}{dt} = \beta \cdot ^\circ C/s \). The final measurement time, \( t_F \), is the final temperature, \( T_F \), divided by the heating rate, \( \beta \).

### 4.2. Model parameter values

The behavior of Eq. (1) is sensitive to the parameter values chosen. In this section, we describe the values used in this study. While all of the values presented here are consistent with available literature values and with experimental results, it should be stressed that many of these values will vary between samples. The careful quantification of these parameters will be prerequisite for the quantification of thermal histories using feldspar TL signals.

#### 4.2.1. Geologic \((D_C)\) and laboratory \((D_L)\) dose rates

The average environmental dose rate for all samples is 4.0 ± 1.5 Gy/ka, represented by our chosen \(D_C\) value of 4 Gy/ka. The laboratory dose rate, \(D_L\), administered by the \(^{90}Sr/^{90}Y\) beta source at UCLA has been measured to be 0.1 Gy/s at the sample location using the standard calibration quartz sample supplied from Risø DTU National Laboratory. This value is used to simulate laboratory irradiations.

#### 4.2.2. Characteristic dose, \(D_0\)

The TL dose response of sample J1012 is shown in Fig. 5a following single-aliquot regenerative doses ranging from 0 to 3.9 kGy. Because we are concerned with growth in the region of the TL curve near the natural \(T_{1/2}\) values, we examine the saturation behavior around the 230°C region of the glow curves \((T_{1/2} = 223, 227,\) and 236°C for J1012; purple TL curves in Fig. 2). Specifically, we fit the TL values to a single saturating exponential function of the form

\[
I = I_{\text{max}} \left(1 - \exp^{-D/D_0}\right)
\]

where \(I\) is the TL intensity which increases with given dose \(D\) up to some maximum intensity \(I_{\text{max}}\) (Christodoulides et al., 1971). In this region, we see an average \(D_0\) value of 1.6 kGy. Such a value is consistent with previous additive-dose observations (e.g., Balescu and Lamothe, 1992; Balescu et al., 1997).

Given the multiple-aliquot additive-dose (MAAD) results reported in Section 3.2, it appears as though the TL intensity at the natural \(T_{1/2}\) value derives from those traps which will remain only partially filled \((n/N < 0.86)\) at the relevant geologic dose-rate and temperature. In this view, a conservative approach would be to examine the dose-responses at more stable portions of the curve to avoid measuring traps that would fill at laboratory but not geologic dose-rates. We therefore report a \(D_0\) value of 1.6 kGy, a value taken from the range 260 < \(T(°C)\) < 270.

Ultimately, this parameter will control the time required for a sample to equilibrate to thermal steady-state and should therefore be quantified thoroughly when addressing transient responses to thermal perturbation. For our study, where sites have been cooling very slowly for at least 10 Ma \((t \gg 2D_0/D)\), this parameter will only marginally affect our drill core fitting results. In rapidly-cooling bedrock, however, this term will influence the length of time that traps will remain in disequilibrium.

#### 4.2.3. Frequency factors, \(P_0\) and \(s\)

For the attempt-to-tunnel and attempt-to-escape frequency factors \((P_0\) and \(s\), respectively) we use a reasonable but arbitrary value of \(2 \times 10^{16} \text{s}^{-1}\). Post-isothermal TL analyses (Brown and Rhodes, 2017) of J1012 suggest that the effective frequency factors involved in TL production, i.e., \(P(t')/P(t') + s\) term within Equation (1), range from \(10^{14}\) to \(10^{18} \text{s}^{-1}\), decreasing monotonically as a function of isothermal holding temperature or duration.

Despite the fact that the \(P_0\) and \(s\) values have different physical meanings (pp. 48–49, Mckeever, 1985; Tsuchiya et al., 1987) and may vary by orders of magnitude (Jain et al., 2015), we assign them the same numerical value for goodness-of-fit and simplicity (we express both terms individually in Equation (1)).

#### 4.2.4. Activation energy, \(\Delta E\), and recombination center density, \(\rho'\)

Jain et al. (2015) introduced the following expression to describe isothermal TL from feldspars:

\[
L = -\frac{dn}{dt} = 3n_0\rho'z(t')^{-1} \left(\ln(t'P_0) - \delta\right)^2 \exp\left(-\rho'(\ln(t'P_0) - \delta)^3\right)
\]

where \(t' = t_0 + zt\) and \(\delta = \Delta E/k_B T\) with \(n_0\) representing the concentration of trapped electrons at the start of the measurement and \(z\) representing the rate of change for the lifetime of trapped charge (following Huntley (2006) and Jain et al. (2012), we set \(z = 1.8\)). The variable \(t_0\) represents the critical lifetime at the start of the measurement. Both \(n_0\) and \(t_0\) depend upon the radiation history of a sample and are best-fit parameters. Assuming that recombination proceeds by tunneling from the excited state to randomly-
distributed luminescence centers, isothermal TL at any hold temperature should approximately follow Eq. (6).

Fig. 5b shows the isothermal decay of an aliquot of J1012 held at 250, 300, and 350°C for 1000 s (400 s of which is shown). These data are fitted with Eq. (6) using the same parameters used in the main text to fit the T1/2 values for all drill core samples at natural and laboratory conditions, namely: $\Delta E = 1.3$ eV, $\rho' = 1.32 \times 10^{-3}$ and $P_0 = 2 \times 10^{16}$ s$^{-1}$.

4.3. Simulated TL responses following isothermal geologic histories

Using Eq. (1) and the parameter values listed in Table 2 (with the average geologic dose rate $D_G$ for all samples of 4 Gy/ka), we modelled the evolution of $n(r')$ for hold temperatures of 0, 10, and 20°C, and durations of 20 ka, 200 ka, and 2 Ma. After 800 ka ($2D_0/D_G$), assuming the parameters listed in Table 2, the most stable traps (highest $r'$ values) will be effectively saturated, i.e., $n/N \sim 0.86$ (see also Fig. 7). After 2 Ma, these traps should be entirely full ($n/N \sim 1$). The final distribution of $n(r')$ after each treatment was then evaluated using Eq. (4) to produce a synthetic TL curve; these are shown in Fig. 6a.

Two features are remarkable. First, and most relevant for this study, the TL peaks are emitted at higher stimulation temperatures when trapping occurs at higher temperatures. This is because those sites which are nearer to centers (i.e., have lower $r'$ values) are unstable at higher ambient temperatures, and are therefore empty during the natural TL measurement. Second, the integrated emissions are greater for those simulations at lower temperatures. The reason for this is that the ratio of excited-to-ground-state electrons ($n_e/n_g$) depends exponentially on temperature ($n_e/n_g = \exp(-\Delta E/k_BT)$) and this ratio controls the rate of detrapping (see the Supplementary Materials for more detail).

4.4. Simulated TL responses following isothermal treatments

The same approach was used to predict the effects of short duration heat treatments. For each of these simulations, laboratory irradiation was reproduced by changing the dose rate, $D$, to 0.1 Gy/s (this mimics the dose-rate received by crystals exposed to the $^{40}$Sr/$^{88}$Y beta source at UCLA) and allowing the $n(r')$ distribution to evolve for 200 s (a simulated laboratory dose of 20 Gy) at 20°C. Next, this $n(r')$ distribution was used as the initial condition of an isothermal heat treatment. The simulated hold times were 100, 300, and 1000 s; and the temperatures were 100, 150, and 200°C. Finally, the $n(r')$ distribution was evaluated with Eq. (4), producing the TL curves shown in Fig. 6c.

The effects of heating are to shift the TL emissions to higher measurement temperatures and to reduce the peak intensity. This reason for this behavior is the progressive thermal erosion of those sites which have lower recombination distances; the more stable sites comprise the higher temperature regions of the TL measurements.

4.5. Trapping at a single recombination distance

Equation (1) can also be used to illustrate the evolution of trap populations under different scenarios. An arbitrary recombination distance of $r'$ (e.g., 1.5) and a constant temperature of $-4.1$ °C (e.g., sample J1012) are examined within a 2 Ma simulation (Fig. 7a). The results are shown as the fraction of traps which are filled (when $n/N = 1$, all available traps are filled). Once about 86% of traps are filled, even small variations in the measured luminescence response will lead to large or infinite errors in age determination and the trap is effectively saturated (Wintle and Murray, 2006). This saturation level is described with the $D_0$ parameter (effective saturation occurring at doses $> 2D_0$). In our case, we prescribe a value of $D_0 = 1.5$ kGy based on dose response measurements of sample J1012 (Fig. 5a); higher values result in a greater time required to reach saturation.

In our simulation, trap filling through time progresses as expected for a discrete trap (Fig. 7a). As the available sites fill, the fractional saturation behaves as a saturating exponential function. Notice that at the chosen temperature, this site will not fill entirely ($n/N < 1$). In other words, a thermal steady-state $\left(\left(n/N\right)_{SS}\right)$ is reached which is incompletely saturated (cf. Christodoulides et al., 1971). Of course, with randomly distributed luminescence centers many recombination distances will occur, as discussed in the following section.

4.6. Trapping at all recombination distances

Considering all recombination distances present in the lattice and assuming randomly distributed centers, we can visualize trapping as a function of both time and recombination distance. Using Eq. (1), trapping is simulated at $T = -4.1$ °C for durations of 0.25, 0.5, 1, and 2 Ma (Fig. 7b). The results shown in Fig. 7a are indicated with the light blue line for reference. Those traps with centers nearer than about $r' = 1.7$ will not saturate completely (given the prescribed temperature and dose rate) and sites at $r' \leq 0.8$ will not accumulate a significant concentration of electrons. Such sites would accumulate appreciable charge, however, if the temperature were lowered sufficiently. Nevertheless, after 2 Ma all sites are in thermal steady-state $\left(\left(n/N\right)_{SS}\right)$ and their concentrations will not change until the temperature changes.

4.7. Trapping at drill core temperatures

Finally, the simulation conducted in Section 4.6 is repeated for the steady-state temperatures experienced by drill core samples J1012, J1026, and J1030 ($T_{SS} = -4.1, 19.8,$ and $55.1$ °C, respectively) (Fig. 7c). The $r'$ values greater than about 1.48 reach effective saturation ($n/N > 0.86$) after some amount of time (in this example, sites nearer to centers than $r' = 1.48$ experience thermally-assisted tunneling at a rate higher than the filling rate). The more stable sites saturate after 800 ka, but some of the less stable sites reach saturation later. This is because the detrapping rate is greater for

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$D$</td>
<td>Dose rate</td>
<td>4 Gy-ka$^{-1}$ (geologic) or 0.1 Gy-s$^{-1}$ (laboratory)</td>
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<tr>
<td>$D_0$</td>
<td>Characteristic dose</td>
<td>1.6 kGy</td>
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<tr>
<td>$\Delta E$</td>
<td>Activation energy to excited state</td>
<td>1.3 eV</td>
</tr>
<tr>
<td>$P_0$, s</td>
<td>Frequency factors</td>
<td>$2 \times 10^{16}$ s$^{-1}$</td>
</tr>
<tr>
<td>$\rho'$</td>
<td>Dimensionless recombination center density</td>
<td>$1.32 \times 10^{-3}$</td>
</tr>
</tbody>
</table>
these sites. Higher mean temperatures result in a trapped population with greater minimum $r'$ values. In other words, the nearer sites that would be occupied at lower temperatures remain empty at higher temperatures. This trend in site occupancy with temperature can be examined in the measured TL signals from drill core samples, which is discussed in the following section.

5. Comparing measured and modeled behaviors

5.1. Comparing natural signals to modeled signals

The $T_{1/2}$ values for all drill core natural TL signals are shown as open symbols in Fig. 6b. Also shown as a solid black curve in Fig. 6b are the $T_{1/2}$ values simulated at natural conditions. To produce these values, we first solve Eq. (1) for the time range $t = 0$ to 2 Ma at each sample's burial temperature, $T_{SS}$. The resulting $n(r')$ distribution for each sample is evaluated with Eq. (4) to determine the TL that would result after burial at $T_{SS}$ for 2 Ma. A remarkable correlation is found, suggesting that the measured relationship between natural $T_{1/2}$ values and the steady-state temperature is explainable in terms of site stability.

5.2. Comparing isothermal decay of TL signals to modeled response

The $T_{1/2}$ values following laboratory irradiation and heat treatment are plotted as open symbols in Fig. 6d. Also plotted are the $T_{1/2}$ values that are simulated with Eqs. (1) and (4), given the same kinetic parameters used in Fig. 6b. It is encouraging that the same kinetic parameters that reproduce the natural drill core $T_{1/2}$ values also resemble the high-temperature measurements.

This correlation between measured and simulated $T_{1/2}$ values gets stronger at longer durations and higher temperatures, which may suggest that our model fails to incorporate transient luminescence phenomena occurring at room temperature. Ground-state tunneling is omitted from the current model, but this effect should only decrease the minimum stability distance, shifting the $T_{1/2}$ value higher. This discrepancy deserves further consideration.

6. Discussion and conclusions

Thermoluminescence signals from bedrock feldspars show a systematic dependence on ambient temperature. During burial, the electron traps within these crystals were filled according to the stability of each trapping site. Because this stability should depend on the distance to the nearest recombination center, a distribution of trap saturation as a function of distance develops, $n(r')$, which characterizes a samples thermal history. In the case of thermal steady-state, some sites are entirely filled ($n/N \sim 1$), some are partially filled, and some remain empty (Fig. 7b). This partially-occupied recombination distance controls the position of the $T_{1/2}$ measurements shown for the natural signals and for signals following isothermal treatments (Fig. 6b and d).

The systematic dependence of natural $T_{1/2}$ values on ambient temperature (Fig. 6b) coupled with the multiple-additive dose results (Fig. 3) imply that $T_{SS}$ controls trapping site occupancy and therefore the natural shape of feldspar TL, a behavior that can be explained in light of recent advances in our understanding of feldspar luminescence kinetics (e.g., Jain et al., 2015; Pagonis et al., 2016). Within this context, the role of anomalous fading should be considered. In our formulation (Eq. (1)), fading is incorporated, though only in the excited-state (i.e., thermally-assisted tunneling). Thermally-activated tunneling can produce the phenomenon of anomalous fading as commonly measured in sediment studies (e.g., a decrease in luminescence intensity after storage at room
temperature; Huntley and Lamothe, 2001), though with current parameter values, the magnitude of simulated room temperature fading is much lower than is experimentally observed. The observed fading rate will depend primarily upon the activation energy required to access the excited state, the ambient temperature, the effective frequency factor, and the density of recombination centers.

Of particular note is the agreement that we observe between model predictions and measured TL responses following natural and high-temperature laboratory heating conditions (Fig. 6). The same kinetic parameters (Table 2) described in Section 4.2 can be evaluated with Eq. (1) to reproduce the T_{1/2} position resulting from 1000 s at 200°C (T_{1/2} offset by 15°C; Fig. 6d) and thermal steady-state (t \approx order 10^5 ka) at -4.1°C (T_{1/2} offset by 5°C; Fig. 6b).

We emphasize that this model is one of the simplest justifiable models for feldspar luminescence. Additional pathways that could be incorporated in the future might include activation into the band-tail states (up to the conduction band) or ground-state tunneling, both of which have been adopted for IRSL thermochronometry with feldspars (e.g., Guralnik et al., 2015b; King et al., 2016b). The main elements of this kinetic model are identical to those used in Jain et al. (2015) and have been used in that and other studies (Kitis and Pagonis, 2013; Pagonis et al., 2016) to explain both optical and thermal features of feldspar luminescence. Thermoluminescence signals may be preferable over optical luminescence for feldspar thermochronology applications, however, as the full range of thermal stability is monitored during a single TL measurement. Additionally, TL measurements avoid the complications arising from preheating and phototransfer effects.

Moving forward, many questions remain to fully develop this method. Does the feldspar TL response become more sensitive to radiation with prolonged heating or metamorphism? Both the TL shape change after heating to 500°C (Brown, 2017) and the observation that the degree of feldspar ordering correlates with the degree of fading (p. 185; Aitken, 1983; Visecek et al., 1994) suggest that peak metamorphic conditions may influence the subsequent rate of charge accumulation. What is the maximum steady-state temperature that can be identified using the leading edge of TL emissions? In core W219, the natural TL signals were too low to resolve the T_{1/2} value at T \geq 23.0°C, whereas for core R716, all samples gave useful TL signals, up to the highest temperatures measured: 60.2°C. How should one handle low-temperature shoulders when identifying the natural T_{1/2} value? It may be useful to separate shoulders by curve deconvolution, for example. Can we analytically define the closure temperature for a TL age resulting from different geothermal scenarios, or can this only be defined numerically? What is the natural variation for the parameters of Table 2? Efforts are underway currently to explore this variation for both optical and thermal signals in feldspars (Sampa et al., 2015; Guralnik et al., 2015b; Valla et al., 2016; Brown and Rhodes, 2017). Is excited-state tunneling to randomly-distributed luminescence centers the primary detrapping pathway at geologic conditions? For example, initial simulations of linear cooling scenarios (not shown here) indicate that the TL system presented here may remain in thermal disequilibrium at cooling rates as slow as about 10°C/Ma, but this result depends strongly on the parameter values chosen as well as the incorporated recombination pathways.

Our results illustrate the potential utility of the feldspar TL signal for geothermal studies. The n(r') distribution is sensitive to a wide range of ambient temperatures: -4.1 – 60.2°C. This distribution responds to thermally dynamic scenarios as well and initial simulations suggest that the signal should be useful for monitoring rapid exhumation during the Quaternary. This combination of low-temperature sensitivity and measurable signal growth between 10^2 to 10^4 years is promising for tectonic and geomorphic applications involving short-wavelength, upper-crustal thermal perturbations, and could prove useful in resolving questions of recent bedrock exhumation rates.

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